

For non-radiating or stable states, the relationship between the electron wavelength and the allowed radii is:

$$2\pi[nr_{(1)}] = 2\pi r_{(n)} = n\lambda_{(1)} = \lambda_{(n)} \quad (2)$$

where  $n = 1$

or  $n = 2, 3, 4 \dots\dots\dots$

or  $n = 1/2, 1/3, 1/4 \dots\dots\dots$

and  $\lambda_{(1)}$  = the allowed wavelength for  $n = 1$

$r_{(1)}$  = the allowed radius for  $n = 1$

In a hydrogen atom (and the following applies equally to a deuterium atom), the ground state electron-path radius can be defined as  $r_{(0)}$ . This is sometimes referred to as the Bohr radius,  $a_0$ . There is normally no spontaneous photon emission from a ground state atom and thus there must be a balance between the centripetal and the electric forces present. Thus:

$$[m_{(e)} \cdot v_1^2] / r_{(0)} = Ze^2 / (4\pi \cdot \epsilon_{(0)} \cdot r_{(0)}^2) \quad (3)$$

- where  $m_{(e)}$  = electron rest mass
- $v_1$  = ground state electron velocity
- $e$  = elementary charge
- $\epsilon_{(0)}$  = electric constant  
(sometimes referred to as the permittivity of free space)
- $Z$  = atomic number (for hydrogen, 1)

Looking first at the excited (higher energy) states, where the hydrogen atom has absorbed photon(s) of discrete wavelength/frequency (and hence energy), the system is again stable and normally non-radiating, and to maintain force balance, the effective nuclear charge becomes  $Z_{eff} = Z/n$ , and the balance equation becomes:

$$[m_{(e)} \cdot v_n^2] / nr_{(0)} = [e^2/n] / (4\pi \cdot \epsilon_{(0)} \cdot [nr_{(0)}]^2) \quad (4)$$